such that the distances from any point on the hyperbola to the foci differ by 6.

Do NOT solve this problem using symbols in place of the numbers given.

$$\left| \sqrt{x^2 + (y+12)^2} - \sqrt{x^2 + (y-12)^2} \right| = 6$$

$$\sqrt{x^2 + (y+12)^2} - \sqrt{x^2 + (y-12)^2} = \pm 6$$

OF SUBTRACTION WAS REVERSED

$$\sqrt{x^2 + (y+12)^2} = \pm 6 + \sqrt{x^2 + (y-12)^2}$$

$$48y - 36 = \pm 12\sqrt{x^2 + y^2 - 24y + 144}$$

$$4y-3 = \pm \sqrt{x^2 + y^2 - 24y + 144}$$

$$16y^2 - 24y + 9 = x^2 + y^2 - 24y + 144$$

$$15y^2 - x^2 = 135$$

$$\frac{y^2}{9} - \frac{x^2}{135} = 1$$

Convert the rectangular equation y = 3x - 5 to polar form. Write r as function of θ , and simplify your answer. SCORE: _____/4 PTS

 $r \sin \theta = 3r \cos \theta - 5$

 $r\sin\theta - 3r\cos\theta = -5$

$$r\sin\theta - 3r\cos\theta = -5$$

$$r(\sin\theta - 3\cos\theta) = -5$$



 $r = \frac{-5}{\sin\theta - 3\cos\theta} = \frac{5}{3\cos\theta - \sin\theta}$ If therasum of

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[b]

SCORE: /7 PTS

A house has an exposed (straight) beam 25 feet above and parallel to the floor. Two small lamps hang from the ceiling. [a]

There is an arch such that the total distance from one lamp to any point on the arch to the other lamp is exactly 18 feet.

The shape of the arch is a/an FLLIPSE (or part of it).

The shape of the graph of the equation $3x^2 + 3x + 2y^2 - 2y - 1 = 0$ is a/an 1 = 1 + 1 = 0

The shape of the graph of the equation $4x^2 + 2x - 3y^2 - 3y - 1 = 0$ is a/an $\frac{1}{2}$ [c]

- The polar co-ordinates $(-5, \frac{3\pi}{7})$ refer to the same point as the polar co-ordinates $(5, \frac{1077}{7})$. (Your answer must be **positive**.) [e]
- The polar co-ordinates $(5, \frac{3\pi}{7})$ refer to the same point as the polar co-ordinates $(5, \frac{117}{7})$. (Your answer must be <u>negative</u>.) [f]
- The point with polar co-ordinates $(-5, -\frac{4\pi}{3})$ lies in quadrant [g]

Convert the polar equation $r^2 = \cos 2\theta$ to rectangular form.

SCORE: /4 PTS

Simplify your answer so that there are no radicals, complex fractions, fractional exponents nor negative exponents.

$$r^2 = \cos^2 \theta - \sin^2 \theta$$

$$r^{2} = \left(\frac{x}{r}\right)^{2} - \left(\frac{y}{r}\right)^{2}$$

$$r^2 = \frac{x^2}{r^2} - \frac{y^2}{r^2}$$

$$r^2 \quad r^2$$

$$r^4 = x^2 - y^2$$

$$\frac{x^4 = x^2 - y^2}{(x^2 + y^2)^2 = x^2 - y^2}$$

$$r^2 = \cos^2 \theta - \sin^2 \theta$$

$$r^2r^2 = r^2(\cos^2\theta - \sin^2\theta)$$

$$r^4 = r^2 \cos^2 \theta - r^2 \sin^2 \theta$$

$$r^4 = x^2 - y^2$$

$$r^{4} = x^{2} - y^{2}$$

$$(x^{2} + y^{2})^{2} = x^{2} - y^{2}$$

GRADE AGAINST

ONLY ONE

VERSION OF

SOLUTION

Find the foci, and equations of the asymptotes of the hyperbola $x^2 - 2y^2 - 6x - 16y - 17 = 0$.

SCORE: /5 PTS

$$(x^2 - 6x) - 2(y^2 + 8y) = 17$$

$$(x^2 - 6x + 9) - 2(y^2 + 8y + 16) = 17 + 9 - 32$$

$$(x^{2} - 6x) - 2(y^{2} + 8y) = 17$$

$$(x^{2} - 6x + 9) - 2(y^{2} + 8y + 16) = 17 + 9 - 32$$

$$(x - 3)^{2} - 2(y + 4)^{2} = -6$$

$$(y + 4)^{2} - (x - 3)^{2} = 1$$

$$c^2 = 3 + 6 = 9 \implies c = 3$$

slopes of asymptotes
$$=\pm\sqrt{\frac{3}{6}}=\pm\sqrt{\frac{1}{2}}=\pm\frac{\sqrt{2}}{2}$$

$$(3, -4 \pm 3) = (3, -7), (3, -1)$$

FOCI: $(3, -4 \pm 3) = (3, -7), (3, -1)$ ASYMPTOTES: $y + 4 = \pm \frac{\sqrt{2}}{2}(x - 3)$



ALTERNATE SOLUTION

$$\begin{vmatrix}
\sqrt{x^2 + (y - 12)^2} - \sqrt{x^2 + (y + 12)^2} &| = 6 \\
\sqrt{x^2 + (y - 12)^2} - \sqrt{x^2 + (y + 12)^2} &| = \pm 6 \\
\sqrt{x^2 + (y - 12)^2} &| = \pm 6 + \sqrt{x^2 + (y + 12)^2}
\end{vmatrix}$$

$$x^2 + y^2 - 24y + 144 = 36 \pm 12\sqrt{x^2 + y^2 + 24y + 144} + x^2 + y^2 + 24y + 144$$

$$-48y - 36 = \pm 12\sqrt{x^2 + y^2 + 24y + 144}$$



$$-4y-3 = \pm \sqrt{x^2 + y^2 + 24y + 144}$$

$$16y^2 + 24y + 9 = x^2 + y^2 + 24y + 144$$

$$15y^2 - x^2 = 135$$

ERNATE SOLUTION